



Distributed Storage Systems: Data Replication using Quorums





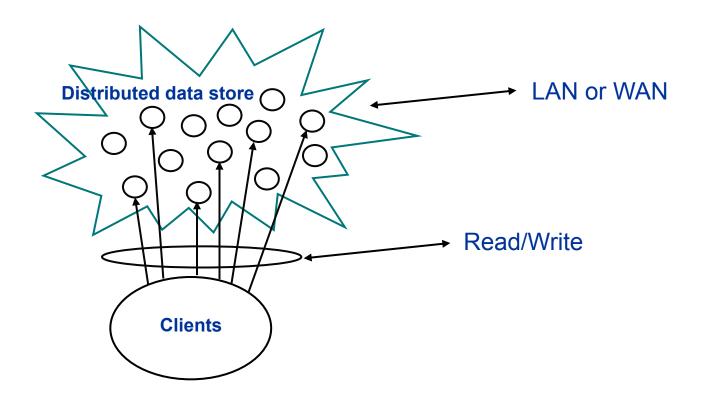
Background

- Software replication focuses on dependability of computations
- What if we are primarily concerned with integrity and availability (and perhaps confidentiality) of data?
- Data replication has several advantages
 - Simpler protocols (atomic ordering not necessarily required, no determinism assumptions)
 - Variety of consistency models provides efficiency/consistency tradeoffs
 - Performance better than software replication: simpler protocols can be implemented efficiently; caching and hashing





Distributed Storage Model







Basic Quorum Systems

- Gifford, "Weighted Voting for Replicated Data," SOSP Proceedings, 1979
- each client reads from r servers and writes to w servers
- if r+w>n, then the intersection of every pair of read/write sets is non-empty ⇒ every read will see at least one copy of the latest value written
- r=1 and w=n ⇒ full replication (write-all, read-one): undesirable when servers can be unavailable because writes are not guaranteed to complete
- best performance (throughput/availability) when 1 < r < w < n, because reads are more frequent than writes in most applications
- generalization: r, w vary across clients but non-empty intersection between all read/write sets is maintained





Basic Quorum Systems: Protocols

- time stamps are maintained for each object in store
- read protocol for a data object V:
 - read <v, t> from all servers in some read set
 - select v with latest time stamp t
- write protocol for a data object V:
 - read value according to above protocol to determine current time stamp t
 - write $\langle v, t' \rangle$ to all servers in some write set with time stamp t' > t
- guarantees serial consistency (sometimes called safe semantics): a read operation that is not concurrent with any write operation on the same object returns the last value written in some serialization of the preceding writes to that object





Serial Consistency

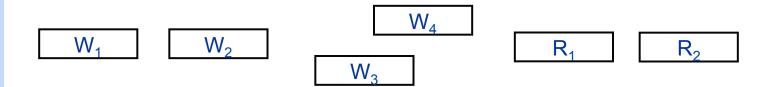
				R₁		
W_1	W_2	W_3			_	W_4
			•	R_2		

(R₁, R₂ both read value written by W₃)





Serial Consistency, cont.



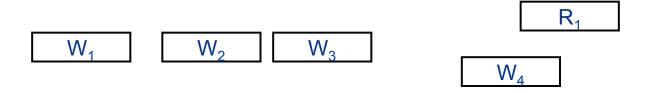
 $(R_1, R_2 \text{ both read } same \text{ value, could be either the result of } W_3 \text{ or } W_4, i.e. serialization could be W_1, W_2, W_3, W_4 \text{ or } W_1, W_2, W_4, W_3 \text{ but it must be seen the same way by } R_1 \text{ and } R_2)$

- how can this be achieved?
- how are timestamps for W₃ and W₄ set?





Serial Consistency, cont.



(R_1 can return *either* the value written by W_4 *or* the value written by W_3 - serial consistency does not cover the case of a read that overlaps with a write)





Data Replication: Performance Optimizations

- Data objects can be large, e.g. files, and many copies are transmitted during quorum protocol operation ⇒ extremely high bandwidth usage
- Hashing
 - Store hash of data at every server along with data
 - Return hash values and meta data (not data) during read operations
 - Do voting based on hash values
 - Once correct hash is determined, query a single server for data object and calculate its hash to verify data integrity
- Caching
 - Store data objects in client caches
 - Execute hashing protocol for a read
 - If object is in cache, calculate hash of cached object and do not query any server for object if cached copy is up to date





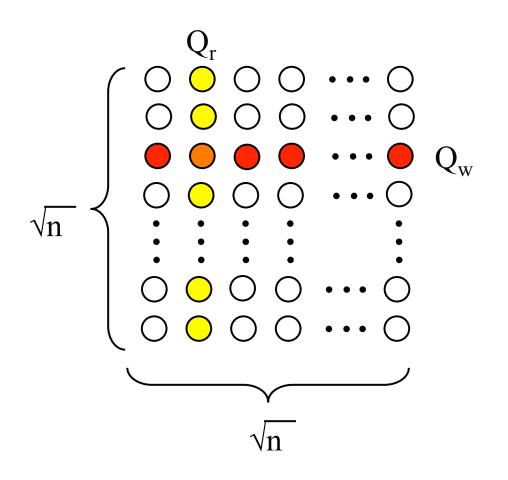
Quorum Systems: Formalization

- assume a set U of servers, where |U| = n
- An asymmetric quorum system \mathcal{Q}_1 , $\mathcal{Q}_2 \subseteq 2^U$ is a pair of non-empty sets of subsets of U, where $\forall Q_r \in \mathcal{Q}_1$, $Q_w \in \mathcal{Q}_2$, $Q_r \cap Q_w \neq \emptyset$
- A symmetric quorum system $\mathcal{Q} \subseteq 2^U$ is a non-empty set of subsets of U, where $\forall Q_1, Q_2 \in \mathcal{Q}, Q_1 \cap Q_2 \neq \emptyset$ (read sets and write sets are identical)
- each $Q \in \mathcal{Q}$ is called a *quorum* (for asymmetric system, there are *read quorums* and *write quorums*)





Efficiency of Quorums: Grid Quorums



Grid Quorums are
Asymmetric
Quorum
Systems!!





System Load

- load = avg. fraction of servers that must be contacted per read/write operation
- for grid quorum systems:
 - load = $\sqrt{n} / n = 1 / \sqrt{n}$
 - load \rightarrow 0 as n \rightarrow ∞
- compare to basic quorum systems:
 - load = (cr + (1-c) w) / n ≥ b, where c is fraction of ops that are reads, b is a constant, and r+w > n





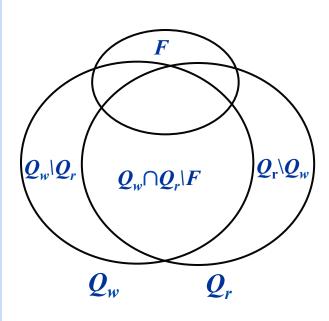
Byzantine Quorum Systems

- Malkhi and Reiter, Distributed Computing
- uses asynchronous system model and assumes servers can fail or be compromised, i.e. servers can experience Byzantine faults
- increase the size of the quorums' intersection to mask responses from faulty servers
- if intersection is at least $2f_{\rm max}$ +1, where $f_{\rm max}$ is max. number of faulty servers, then $f_{\rm max}$ +1 correct servers will match in any Q
- problem: with asynchronous system model, can not distinguish slow servers from faulty servers





Masking Quorum Systems



- $|(Q_w \cap Q_r) \setminus F| = f_{max} + 1$ (correct, upto-date)
- Q_r\Q_w can be out of date and F can be arbitrary
- if f_{max} faulty servers match out-ofdate values in Q_r\Q_w, then f_{max}+1 or more matching old values can exist
- not sufficient to accept the first f_{max}
 +1 values that match





Masking Quorum Systems (cont.)

- suppose a read operation has returned f_{max} +1 values that match but some values have not yet been returned
- if the servers that have not responded are correct but slow, the result might change after more values arrive; if the nonresponding servers are faulty, they might never respond
- if *all* responses arrive from a quorum, pick the newest value that has at least f_{max} +1 representatives (in some cases, correct result can be determined without waiting for all responses)
- approach needs additional constraint: a quorum consisting solely of correct servers must exist at all times to ensure progress
- can contact all servers initially to guarantee a quorum of responses, or can contact different quorums sequentially until a full quorum responds





f-Masking Quorum Systems

- read protocol for a data object V:
 - read $\langle v,t \rangle$ from any $|Q_r| + f_{\text{max}}$ servers in U
 - wait until $|Q_r|$ responses have been received from some quorum Q_r
 - select value with latest time stamp that has at least f_{max} +1 representatives
- write protocol for a data object *V*:
 - read value according to above protocol to determine current time stamp t
 - write <v,t'> to all servers in some quorum Q_w with time stamp t'>t
- guarantees serial consistency as long as a "fullycorrect" quorum exists at all times





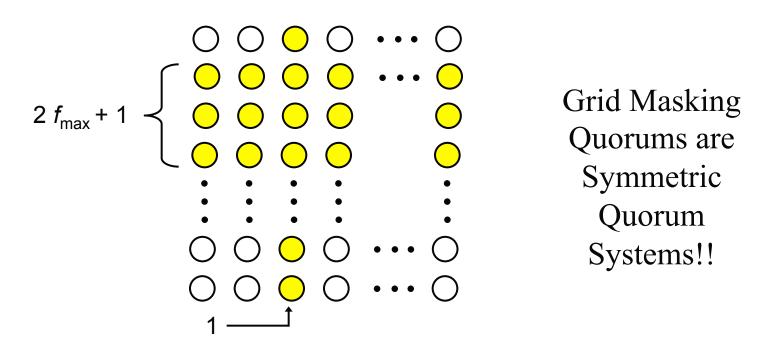
f-Masking Quorums: Sufficient Condition

- if n > 4 f_{max} and a symmetric quorum system is used with $|Q_r| = |Q_w| = \lceil (n+2 f_{\text{max}} + 1)/2 \rceil$, then the preceding read/write protocols are correct and guarantee progress
- $|Q_{\mathsf{w}} \cap Q_{\mathsf{r}}| \ge 2 f_{\mathsf{max}} + 1$
- n > 4 $f_{\text{max}} \Rightarrow \lceil (n+2 f_{\text{max}} + 1)/2 \rceil \le n-f_{\text{max}} \Rightarrow \text{at least}$ one "fully correct" quorum exists at all time





Grid Masking Quorum Systems



• quorum is any 2 f_{max} + 1 rows and 1 column of servers \Rightarrow intersection between any 2 quorums \geq 2 f_{max} + 1





System Load

- load = avg. fraction of servers that must be contacted per read/ write operation
- for symmetric quorum systems, load = |Q| / n
 - threshold masking load ≈ $(n+2 f_{max}+1) / 2n \in (0.5, 0.75)$
 - grid masking load ≈ (2 f_{max} +2) $n^{1/2}$ / n ∈ O(f_{max} / $n^{1/2}$) → 0 as n → ∞ (for small f_{max})
- for asymmetric quorum systems, load depends on frequency of reads vs. writes,

load =
$$[c|Q_r| + (1-c)|Q_w|]/n$$
,

where c = fraction of accesses that are reads

- write-all, read-one load = 1-c + c/n > 1-c





Byzantine Quorum System Variations

- dissemination quorum systems
 - work with self-verifying data, e.g. signed data
 - sufficient that quorums' intersection contains at least one non-faulty server, i.e intersection size $\geq f_{max}+1$
 - quorum size = $[(n+f_{\text{max}}+1)/2]$, $n > 3 f_{\text{max}}$
- opaque masking quorum systems
 - clients don't need to know f_{max} (harder for adversary to attack system)
 - read protocol simply does a majority vote among responses
 - $n > 5 f_{max}$ (need to outvote faulty + out-of-date servers)
 - load for any opaque masking quorum system > 1/2
- dealing with faulty/malicious clients
 - can not prevent faulty but authorized clients from writing bad data of which they have write permission
 - have servers execute agreement protocol before installing write values to avoid faulty clients from leaving servers in inconsistent state